## GCSE

## Mathematics

| Session: | 2000 June |
| :--- | :--- |
| Type: | Mark scheme |
| Code: | 1662 |

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## Oxford Cambridge and RSA Examinations

RECOGNISING ACHIEVEMENT

## GENERAL CERTIFICATE OF SECONDARY EDUCATION (former Midland Examining Group syllabus) <br> MATHEMATICS (SYLLABUS A)

## MARK SCHEME FOR COMPONENTS <br> TAKEN IN JUNE 2000

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by Examiners. It does not indicate the details of the discussions which took place at an Examiners' meeting before marking commenced.

All Examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the Report on the Examination.

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## Grade Threshold Marks

Candidates' performances were assessed on each component. The minimum level of performance (the threshold mark) was determined for each grade. These thresholds are given below as unscaled marks (i.e. the scale of marks used by the Examiners).

The relevant component thresholds were then related to each other in accordance with the component weightings to fix the overall threshold marks for each option.

| Component Threshold Marks |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Component | Max mark | A | B | C | D | E | F | G | U |  |
|  | 1 | 100 |  |  |  | 60 | 46 | 33 | 20 |  |
| 2 | 100 |  |  |  | 61 | 48 | 36 | 24 |  |  |
| 3 | 100 |  | 68 | 44 | 32 | 20 |  |  |  |  |
| 4 | 100 |  | 73 | 45 | 32 | 19 |  |  |  |  |
|  | 5 | 100 | 51 | 34 | 18 |  |  |  |  |  |
| Coursework | 7 | 100 | 57 | 37 | 18 |  |  |  |  |  |


| Overall Threshold Marks |  |  |  |  | Option $1+2+7$ (Foundation) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Max Mark | A* | A | B | C | D | E | F | G | U |
| 250 |  |  |  |  | 156 | 122 | 89 | 56 |  |
| Percentage of Candidates <br> Awarded each Grade <br> Total Candidature: 13741 |  |  |  |  |  |  |  |  |  |
|  | $\mathrm{A}^{*}$ | A | B | C | D | E | F | G | U |
| Percentage in Grade |  |  |  |  | 13.6 | 36.1 | 33.2 | 14.7 |  |
| Cumulative \% in Grade |  |  |  |  | 13.6 | 49.7 | 82.9 | 97.6 |  |


| Overall Threshold Marks |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | Max Mark | A* | A | B | C | D | E | F | G | U |
|  | 250 |  |  | 167 | 109 | 77 | 45 |  |  |  |

Percentage of Candidates
Awarded each Grade
Total Candidature:

|  | A* | A | B | C | D | E | F | G | U |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Percentage in Grade |  |  | 17.6 | 45.6 | 24.3 | 11.3 |  |  |  |
| Cumulative \% in Grade |  |  | 17.6 | 63.2 | 87.5 | 98.8 |  |  |  |


| Overall Threshold Marks |  |  |  |  |  | Option $5+6+7$ (Higher) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Max Mark | $A^{*}$ | A | B | C | D | E | F | G | U |
| 250 | 194 | 143 | 95 | 49 |  |  |  |  |  |
| Percentage of Candidates Awarded each Grade |  |  |  |  |  | Total Candidature: |  |  |  |
|  | A* | A | B | C | D | E | F | G | U |
| Percentage in Grade | 15.3 | 42.3 | 34.6 | 7.6 |  |  |  |  |  |
| Cumulative \% in Grade | 15.3 | 57.6 | 92.2 | 99.8 |  |  |  |  |  |

Markscheme 1662/1 June 2000

RECOGNISING ACHIEVEMENT

|  | Final Marking Scheme Details |  |  |
| :---: | :---: | :---: | :---: |
| 1 | (a) 8209 <br> (b) 473 <br> (c) 179 <br> (d) 2360 <br> (e) 2400 | 1 |  |
| 2 | (a) Tangent <br> (b) Arc <br> (c) Diameter or radius <br> (d) Chord | 1 <br> 1 <br> 1 <br> 1 | MARKING DOWN THE PAGE |
| 3 | (a) $\{(1), 2,4,5,10(20)\}$ <br> (b)(i) 49 <br> (b)(ii) ( $\pm$ ) 9 <br> (c)(i) One of $8,10,12,14,16,18$ <br> (ii) 12 or 18 <br> (iii) 11,13 or 17 . <br> (iv) 8 | 2 <br> 1 <br> 1 <br> 1 <br> 1 <br> 1 <br> 1 | B1 for any 2 correct, with no more than one incorrect. Accept x signs. |
| 4 | 11carnations and 65p change. | 3 | B2 for sight of 11. <br> Or M1 for sight of figs $10 \div$ figs 85 Or for signs of repeated addition Or attempt at multiplying by 85 . e.g. 10 carnations $+£ 1.50$ implies M1 |


| 5 | (a) The Rolling Stones. <br> (b) 80 <br> (c) Not a large enough sample or Not enough sites. <br> Not a uniform cross-section. | 1 <br> 2 <br> S1 <br> C1 | M1 for an attempt to add up the readings. At least 4 of $32,14,18,8,4,2,2$. |
| :---: | :---: | :---: | :---: |
| 6 | £1150 | 5 | If incorrect, then allow B1 for each of the following seen or implied <br> 130 (or two 65's) <br> 300 (or three 100's) <br> 170 <br> 550 If not B 4 then also <br> M1 for adding. |
| 7 | 18 to 20 $\mathrm{cm}^{2}$ | $\stackrel{2}{U 1}$ | B1 for an answer between 17.5 and 22 inclusive. |
| 8 | (a)(i) $\mathbf{2 4 0 0 0 0}$ or $\mathbf{2 3 7 6 0 0}$ or $\mathbf{2 3 2 0 0 0}$ or 237000 <br> (ii) More ; Value(s) we have used are over estimates. <br> (b) 22968 | 2 <br> 1 <br> 3 | M1 for $800 \times 30 \times 10$ seen or implied <br> Or $792 \times 30 \times 10$ or $800 \times 29 \times 10$ <br> Or $790 \times 30 \times 10$ soi. SC1 for figs 24 seen. <br> M1 for showing a desire to multiply 792 by 29 even if also $\times 10$, and M1 for a correct method with only one error. |
| 9 | (a) 7 <br> (b) 6 | $2$ <br> 3 | M1 for placing 8 or 9 of the numbers in order. <br> M1 for attempt to total at least 8 numbers. M1 for - by (their) 9. |
| 10 | (a) $1 / 5 \mathrm{oe}$ <br> (b) $49 / 100$ <br> (c) $31 / 100$ | $\begin{aligned} & 1 \\ & 1 \\ & 2 \end{aligned}$ | Penalise once only for such as 1 out of 5 1 to 5,1 in $5,1: 5$ <br> M1 for sight of 31 or for100 - their total of $20+14+35$ |



| 14 | (a) 24 <br> (b) 110 <br> (c)(i) g <br> (ii) $k$ <br> (iii) d | $\begin{aligned} & 1 \\ & 2 \\ & 1 \\ & 1 \\ & 1 \end{aligned}$ | M1 for 360-100-90-60 |
| :---: | :---: | :---: | :---: |
| $\begin{aligned} & 15 \\ & \mathrm{C} 2 \end{aligned}$ | (a) 31 c.a.o. <br> (b) 1, 6, 11, 2. <br> (c) 281 to 290 <br> (d) 4 sectors correct $\pm 2^{\circ}$ | 1 <br> 2 <br> 1 <br> 4 | NOT 264 to 295 <br> B1 for two totals correct, or all the tallies correct. <br> B1 for each correct sector, ignore labels. OR after B0 or B1, then B2 for two of $18,108,198,36$ or $5,30,55,10 \%$. <br> OR M2 for $360 \div$ her $20 \times$ her f <br> Or $100 \div$ her $20 \times$ her $f$. <br> OR M1 for $360 \div$ her 20 or $100 \div$ her 20 |
| 16 | (a) (I) 3.5 or $31 / 2$ c.a.o. <br> (ii) 6 <br> (iii) 7 <br> (b)(i) $16 q$ <br> (ii) $8 n+4 p$ mark final answer. | 1 <br> 2 <br> 2 <br> 1 <br> 2 | Not $7 / 2$ <br> B1 for $3 x=13+5$ or better, or B1 for correct embedded as their final answer. B1 for $6 x-x=26+9$ or better or B1 for correct embedded as their final answer. <br> B1 for either part seen. |
| $17$ | (a) $3 n$ <br> (b) $4 n+1$ | $\begin{aligned} & 1 \\ & 2 \end{aligned}$ | Ignore $\mathrm{n}=\ldots$.... Allow n3 <br> B1 for 4 n soi. <br> SC1 for $\times 4+1$ |


| 18 C5 | (a) 2 'vertical lines' $\pm 2 \mathrm{~mm}$ <br> 3 'horizontal lines' $\pm 2 \mathrm{~mm}$ <br> Accurate semi-circle $\pm 2 \mathrm{~mm}$ <br> Angles $60 \pm 2^{\circ}$ <br> (b) 20 cm oe. $\operatorname{Or} 0.2 \mathrm{fm}$ or $1 / 5 \mathrm{~m}$. | $\begin{aligned} & \text { V1 } \\ & \text { H1 } \\ & \text { S1 } \\ & \text { A1 } \\ & 2 \end{aligned}$ | Ruled <br> Ruled <br> 'compass' drawn. <br> B1 for 200 seen or $100 \div 5$ |
| :---: | :---: | :---: | :---: |
| 19 |  <br> (a)(i) $-1,2,5,8,11$. <br> (ii) Correct ruled line. <br> (b) (i) $-1,3,15$ <br> (ii) Correct smooth line. | 1 <br> 2 <br> 1 <br> 3 | B1 for 3 or more correctly $\downarrow$ plotted points. <br> B2 Correct points not joined or badly so. <br> B1 Three points correctly plotted. |

RECOGNISING ACHIEVEMENT

Markscheme 1662/2 June 2000

| 1 | (a) 20 (minutes) <br> (b) Britain Today <br> (c) Off the Shelf; World News | $\begin{gathered} 1 \\ 1 \\ 1+1 \end{gathered}$ | Not '30 minutes' | 4 |
| :---: | :---: | :---: | :---: | :---: |
| 2 | (a)(i) One quarter, o.e. <br> (ii) Three eighths, o.e. <br> (b) South <br> (c) $90^{\circ}$ | 1 <br> 1 <br> 1 | Words or figures Allow $\frac{1 \frac{1}{2}}{4} . \operatorname{SC} 1$ for $\frac{3}{4}$ and $\frac{5}{8}$ | 4 |
| 3 | (a)(i) Odd <br> (ii) 17,19 $\text { (b)(i) } \begin{aligned} & 1+3+5+7+9=25 \\ & 1+3+5+7+9+11=36 \end{aligned}$ <br> (ii) Square (numbers) | $\begin{aligned} & \hline 1 \\ & 1 \\ & 1 \\ & 1 \\ & 1 \\ & \hline \end{aligned}$ | For both SC1 for both LHS or both RHS correct <br> Dep on 25 \& 36 not wrong | 5 |
| 4 | $\begin{aligned} & 8 \\ & 11 \\ & 7 \end{aligned}$ | $\begin{aligned} & 1 \\ & 1 \\ & 1 \end{aligned}$ |  | 3 |


| 5 | (a)(i) 40 | 1 |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | (ii) 20 | 1 | Ignore any units |  |
|  | (b)(i) $($ Square $)$ pyramid | 1 | Condone spelling |  |
|  | (ii) $53^{\circ}\left( \pm 2^{\circ}\right)$ | 1 |  |  |
|  | (iii) 4 correct lines drawn | 2 | SC1 for two or three correct \& none wrong |  |
|  | (iv) 4 |  |  |  |


| 6 | (a) 3 points plotted correctly <br> (b)(i) $39^{\circ} \mathrm{C}$ <br> (ii) $-14^{\circ} \mathrm{C}$ <br> (c) $\pm 53^{\circ} \mathrm{C}$ (ft) <br> (d) $\quad 5^{\circ} \mathrm{C}\left( \pm 1^{\circ}\right)$ <br> (e) 7 hours | 2 1 1 1 1 1 | $\pm 1 \mathrm{~mm} \mathrm{SCl}$ for two within tolerance Condone omission of lines <br> ft provided that (b)(i) is $+\&(\mathrm{~b})(\mathrm{ii})$ is - | 7 |
| :---: | :---: | :---: | :---: | :---: |
| 7 | (a) $2 \leqslant h \leqslant 3$ metres <br> (b)(i) 9500 cm <br> (ii) 5 (m) w.w.w. <br> (iii) $104,103.9$ or 103.89 .. <br> (c)(i) 2000000 or 2 m <br> (ii) 2500000 or $2 \frac{1}{2} \mathrm{~m}$ | 1 2 2 1 | M1 for 100-95 seen <br> M1 for $95 \div 0.9144$, implied by digits 103(893) <br> SC1 for 2 and 2.5 , or for 2000000 m and 2500000 m |  |


| 8 | (a) Impossible, unlikely, evens, likely, certain <br> (b)(i) 6 <br> (ii) 5 cao <br> (iii) $\frac{5}{40}, \frac{1}{8}, 0.125$ or $12 \frac{1}{2} \%$ | 2 2 1 2 | SC 1 for just one (compensating) error <br> SC1 for 'from 3 to 9 ' o.e. <br> If a fraction is seen in the answer space, mark it and ignore the rest SCl for $5 \div$ their 40 (must be $\geqslant 32$ ); unlikely; 5 out of $40 ; 5$ in $40 ; 1$ out of $8 ; 1$ in 8. | 7 |
| :---: | :---: | :---: | :---: | :---: |
| 9 | (a) $£ 3.04$ <br> (b) $£ 58.80$ <br> (c) $£ 3.68$ <br> (d) $3.6 \times 10^{11} \mathrm{oe}$ | 2 2 3 | M1 for attempt to by $3 \underline{\&} \times$ by 2 or SCl for 1.52 seen <br> M1 for $0.12 \times 490$ oe, soi by 58.8 or 431.2 Step by step methods must be complete $\&$ convincing to earn the M1 <br> B1 for ( 0. .) 46 seen <br> M1 for $\div 3 \underline{\&} \times 8$, or clear \& complete step by step method <br> 0 if the decimal point in long answer, but condone commas or gaps in the wrong place | 8 |


| 10 | (a) $20 \mathrm{~km} / \mathrm{h}$ <br> (b) Horizontal straight line from $A$ Mark made, or that line ends, at (90, 60) <br> (c) Straight line from their B to correct C <br> (d) 'Slowing down' or 'stopping' oe cao | 1 | $\pm 1 \mathrm{~km} / \mathrm{h}$ <br> Minimum length 2 mm ( 1 small square) <br> Indep $\pm 1 \mathrm{~mm}$ <br> Condone C not labelled <br> Not 'going back home', 'going downhill' or 'stopped' | 5 |
| :---: | :---: | :---: | :---: | :---: |
| 11 | (a) All values correct <br> (b)(i) $\frac{1}{25}, 0.04,4 \%$, cao <br> (ii) $0, \frac{0}{\text { anything }}$, impossible <br> (iii) $\frac{5}{25}, \frac{1}{5}, 0.2,20 \%$ <br> (ft) | 2 1 <br> 1 <br> 2 | B1 for max of 2 errors or omissions <br> All others score 0 <br> ft for 'correct' fraction, decimal or \% from their wrong diagram containing at least one 3 and one 4. <br> I for numerator 5 soi | 6 |


| 12 | (a) 41.28 (francs) <br> (b) (£)2.68 as final answer | 3 3 | M2 for $25.8 \times \frac{160}{100}$ or B 1 for figs 1548 or 4128 seen <br> B2 for 2.67 (.) or 2.68 seen, or M1 for $\frac{25.8}{9.63}$ or $\frac{\text { their () }}{9.63}$ | 6 |
| :---: | :---: | :---: | :---: | :---: |
| 13 | (a)(i) $52\left({ }^{\circ}\right)$ <br> (ii) $32\left({ }^{\circ}\right)$ <br> (b) Rhombus | 2 2 2 | M1 for $180-2 \times 64$ <br> B 1 for 116 seen, in working or diagram <br> Bl for parallelogram, kite or diamond |  |


| 14 |  | $\begin{aligned} & 714 \text { to } 714.2 \\ & \mathrm{~cm}^{2} \\ & 105.8 \text { to } 106(\mathrm{~cm}) \end{aligned}$ | $\begin{gathered} 3 \\ \mathrm{U} 1 \\ 3 \end{gathered}$ | M2 for $20^{2}+\pi \times 10^{2}$ or M1 for $\pi \times 10^{2}$ or for $20^{2}+k \pi$ w.w.w. <br> SC2 for 102.8 to 103 or 108.8 to 109 <br> or M2 for $20+20+3+2 \times \pi \times 10$ <br> or M1 for $2 \times \pi \times 10$ or for $20+20(+3)+k \pi$ <br> $(+3)$ | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 15 |  | $\begin{aligned} & y+5 \text { seen } \\ & 3 y+y+5 \text { oe } \\ & 3 y+y+5=61 \text { or their }(b)=61 \text { oe } \\ & \text { seen } \\ & 14 \end{aligned}$ | 1 <br> 2 <br> B1 <br> B2 | ' $y=\ldots$ ' Ignore units stated throughout question <br> B1 for $3 y+$ their (a) <br> Equation in $y$ with at least 1 further step to solution <br> M1 for their $(b)=61 \& 1$ correct step, or, their $(\mathrm{b})=61$ implied by $(61-5) \div k$ | 6 |
| 16 |  | $\begin{aligned} & 1 \times 913 \\ & 272 \times 619 \end{aligned}$ <br> $\times$ their total of two charges 40 or 91.39 | $\begin{aligned} & \text { M1 } \\ & \text { M1 } \\ & \text { M1 } \\ & \text { A2 } \end{aligned}$ | soi by figs $83 \ldots$ <br> soi by figs $787 \ldots$ <br> Al for figs 9138 to 914 | 5 |
| 17 |  | Idea of sampling. Systematic counting Some attempt at ensuring randomness $0.95$ | $\begin{gathered} \mathrm{W} 1 \\ \mathrm{~V} 1 \\ \mathrm{RI} \\ 3 \end{gathered}$ | e.g. use a tally chart <br> M2 for $\frac{(0 \times 10)+1 \times 6+2 \times 1+4 \times 2+3 \times 2}{10+6+1+1+2}$ or B1 for either 19 seen or denominator 20 | 6 |

TOTAL

RECOGNISING ACHIEVEMENT

# Markscheme 1662/3 June 2000 

June 2000
1662/03 Mathematics Syllabus A
1.
(a) $\frac{12}{25} \quad$ cao
(b) $35(\%) \quad$ cao
(c)(i) (0). 375 cao
(ii) 0.0375
2. (a) 31 cao
(b) $1,6,11,2$
(c) 281 to 290 cao
(d) 4 sectors correct $\pm 2^{\circ}$
[Note : Mark to the best advantage of the candidate]
3. (a)(i) 3.5 or $31 / 2$
(ii) 6

1
2
(iii) 7
(b)(i) $16 q \quad$ cao
(ii) $8 n+4 p$ cao final answer
(c) $x^{2}+5 x+4$ final answer (condone $=0$ if no further)

Mark final answer

M1 for attempt at $3 \div 8$ soi by figs $37(5)$ Note: 0.38 does not necessarily imply M1 their (i) $\div 10$; allow truncation or rounding

B1 for two totals correct or all tallies correct
281 to 290 and/or 11 scores 0
B1 for each correct sector. Ignore labels

## After B0 or B1

B2 for two of $18,108,198,36^{\circ}$ or $5,30,55,10 \%$ or M2 for $360 \times$ their f or $100 \times$ their f seen their 20 their20
or M1 for $\frac{360}{\text { their } 20}$ or $\frac{100}{\text { their } 20}$ seen

B1 for $3 x=13+5$ or better or correct value embedded as final answer
B1 for $6 x-x=26+9$ or better or correct value embedded as final answer

B1 for either part seen
B1 for any two of xx (or better) , $4 \mathrm{x}, 1 \mathrm{x}, 4$ seen from multiplying

Ruled. Within 2 mm of correct posn. top and bottom Ruled. Within 2 mm of correct posn. both sides 'compass' drawn

B1 for 200 or $100 \div 5$ seen

Accept n3 etc ; Allow marks for unsimplified B1 for $4 n$ soi \} expressions eg. $5 n-n+1$ or $\mathbf{S C 1}$ for $\mathrm{x} 4+1$ seen

| 6. | 0.3 oe | 2 | M1 for $1-(0.35+0.2+0.15)$ soi or 1-0.52 or 0.48 seen |
| :---: | :---: | :---: | :---: |
| 7. | (a)(i) 2400 <br> (ii) their(i) $\div 1000$ <br> (b) $5 \quad \mathrm{www}$ | $\begin{aligned} & 2 \\ & \sqrt{1} \\ & 3 \end{aligned}$ | M1 for $40 \times 30 \times 2$ soi by figs 24 Evaluated. M2 for 2000/( $20 \times 20$ ) or M1 for $2000=20 \times 20 \times \mathrm{xh}$ or $\mathbf{B 1}$ for 400 seen |
|  | (a) 'Positive' gradient points 'Tight' oval <br> (b) Scattered Points | $\begin{aligned} & 1 \\ & 1 \\ & 1 \end{aligned}$ | 4 or more points. Ignore lines drawn. Indep. Allow points in a straight line Without correlation |
| 9. | (a) 20 www <br> (b) $1000 \times(4 / 5)$ <br> 800 <br> $200 \mathrm{x}(5 / 100)$ <br> their(10)xtheir(800) <br> 8000 cao <br> ( 8000 ww scores SC3) | 3 <br> M1 <br> A1 <br> M1 <br> M1 <br> A1 |  |
|  | (a)(i) $(6,-5)$ <br> (ii) $\left[\begin{array}{c}4 \\ -6\end{array}\right]$ <br> (b)(i) $(11,-1)$ <br> (ii) $y=3$ oe | $\begin{aligned} & 2 \\ & \sqrt{2} \end{aligned}$ $\begin{aligned} & 2 \\ & 2 \end{aligned}$ | B1 for one correct value in correct place Follow thro' $[$ (i) $]-\left[\begin{array}{l}2 \\ 1\end{array}\right]$ Condone fraction line. -B1 for one 'correct' value in correct place. or for both 'correct' given as a row. eg[4,-6] <br> B1 for one correct value in correct place <br> B1 for $x=3$ or correct line drawn on grid |
|  | 4.5 to 5.5 inclusive www | 2 | M1 for one or more of $5.8,6,36$ or $3.2,3,9$ seen in rounding or 27 seen |
|  | (a) 60 <br> (b) 80 <br> (c) $\frac{\mathrm{f}-32}{0.6} \quad \mathrm{oe}$ | $\begin{aligned} & 2 \\ & 2 \\ & 2 \end{aligned}$ | M1 for 68-32 $=0.6 \mathrm{~d}$ or better oe <br> M1 for $\mathrm{d}-0.6 \mathrm{~d}=32$ or $\mathrm{f}-0.6 \mathrm{f}=32$ or better oe <br> M1 for $\mathrm{f}-32=0.6 \mathrm{~d}$ oe or for $f-32 \div 0.6$ <br> $\mathrm{SC1}$ for $\frac{32-\mathrm{f}}{0.6}$ |



RECOGNISING ACHIEVEMENT


| 6. (a) $y+5$ seen <br> (b) $3 y+y+50 e$ <br> (c) $3 y+y+5=61$ <br> or their $(b)=61$ oe seen 14 | $\begin{aligned} & 2 \\ & \text { B1 } \end{aligned}$ B2 | Ignore units stated throughout question <br> B1 for $3 y+$ their (a) <br> Equation in $y$ with at least 1 further step to solution <br> M1 for their (b) $=61$ and 1 correct step or their $(b)=61$ implied by $\frac{61-5}{k}$ |
| :---: | :---: | :---: |
| 7. (a)(i) $n^{3}$ <br> (ii) 6 ab or 6 ba <br> (b) Final answer $12 x-18$ | $\begin{aligned} & 1 \\ & 1 \\ & 1 \end{aligned}$ |  |
| 8. figs $91 \times 913$ <br> figs $1272 \times 619$ <br> $+5 \% \times$ their total of two charges <br> (£) 91.39 or 91.4 Q | M1 <br> M1 <br> M1 <br> A2 | soi by figs $83 .$. <br> soi by figs $787 \ldots$ <br> A1 for figs 9138 to 914 <br> SC2 for 91.39 or $91.4 \underline{0}$ with no working or SC1 for figs 9138 to 914 with no working |
| 9. (a) Two-way table with boys/girls Columns for WP, SS, both, neither oe <br> One way table or questionnaire <br> Gender column or box <br> Columns or boxes for WP \& SS <br> (b) $0.95, \frac{19}{20}$ | T1 <br> C2 <br> T1 <br> C1 <br> 3 | gender column <br> Must allow for negative in order to score C2 <br> C1 for three of these <br> dep on T1 or name or number column soi <br> M2 for $\frac{(0 \times 10)+1 \times 6+2 \times 1+3 \times 1+4 \times 2}{10+6+1+1+2}$ <br> or B1 for either 19 seen or denom 20 |
| 10. (a) 8.04 <br> (b)(i) $7.6149(0$. <br> (ii) 7.61 <br> (iii) $\frac{4^{2}+(0.5)}{4 \times 0.5}, \frac{4^{2}+0.53}{4 \times 0.5}$ <br> 8 to 8.3 |  | ft their (b)(i) which must be at least 3dp SC1 for $\frac{4^{2}+1}{4(\times 1)}$ or $\frac{4^{2}+1}{4 \times 0.5}$ dep on rounding seen in numerator and denominator |

11. Correct trial for $4 \leq x \leq 5$

Improved correct trial for $4<x<5$
Trial for $4.2<x \leq 4.25$
1 All trials evaluated correctly to the first 2 figs (rounded or truncated)
(or trials for both 4.2 and 4.3 with conclusion)

| Answer 4.2 | 1 |  |
| :---: | :---: | :---: |
| 12. (a) (£) 535.95 or 535.96 <br> (b) (£) 376 | $3$ <br> 3 | M2 for $450 \times 1.06^{3}$ soi or B1 for 477 seen M2 for $\frac{319.6}{85}(\times 100)$ soi by figs 376 or M1 for $85 \%=319.6$ or M1 for $k-k \times \frac{15}{100} \approx 319.6, k>368$ |
| 13. Multiplication and subtraction or substitution $\begin{aligned} & x=3 \\ & y=-1 / 2 \end{aligned}$ | M1 <br> A1 <br> A1 | SC2 for both correct but with no valid algebraic manipulation |
| 14. (a) 8.9 to 8.94 <br> (b) 7.7 to 7.75 | 3 <br> 3 | M2 for $\sqrt{\left(12.4^{2}-8.6^{2}\right)}$ or <br> M1 for $x^{2}+8.6^{2}=12.4^{2}$ <br> M2 for 8.6tan(180-138) or equiv. trig method M1 for $\tan (180-138)=\frac{D C}{8.6}$ or equiv. trig |

15. (a) Final answer 10x-22
(b) 1,2,3,4
(c) Final answer $3 x(2 x-3 y)$ or

$$
-3 x(-2 x+3 y)
$$

(d)(i) $(x-6)(x-2)$
(ii) 2,6
16. (a) 83.6 to $84\left({ }^{\circ}\right)$
(b) 1.125 (m)
17. (a)(i) 0.72
(ii) 0.02
(b) Plots at $10,30,50,70,90$

Plots at correct heights
Ruled joins (at least 4 plots)
(c)(i) $4,23,53,71,80$
(ii) Correct ft plots at $20,40,60,80,100$ Curve or ruled joins (at least 4 plots)
(d)(i) 50 to 54 (minutes)
(ii) 27 to 32 (minutes)

2 B1 for $4 x-20+6 x-2$ condoning $\mid$ error
$2 \quad$ B1 for $0<n<14 / 3$ (soi by 4.6(.)) or0, 1,2,3,4 or 1-4 or 1 to 4 or $0<n \leq 4$ or $0 \leq n \leq 4$
2 Condone missing final bracket
B1 for $x(6 x-9 y)$ or $3\left(2 x^{2}-3 x y\right)$ or $6 x(x-1.5 y)$ or $3 x(2 x-3 y)$ or $-3 x(-2 x+3 y)$ seen
$2 \quad$ SC1 for $(x \pm 6)(x \pm 2)$
1 ft ft from their two bracket factors
or for both correct values however obtained
$4 \quad$ B3 for $\mathbf{4 1 . 8}$ to $\mathbf{4 2}$
or M3 for $2 \sin ^{-1} \frac{0.8}{1.2}$ or M2 for $\sin ^{-1} \frac{0.8}{1.2}$
or M1 for $\sin =\frac{0.8}{1.2}$
(M marks available for equivalent trig)
2 M1 for $\frac{x}{1.8}=\frac{1}{1.6}$ oe

2 M 1 for $0.9 \times 0.8$
$2 \quad \mathrm{~B} 1$ for both 0.1 and 0.2 seen
In (b) \& (c) $1 / 2$ small square accuracy for plots and joins
P1 Horizontal time axis with correct linear scate
H1
J1 Ignore joins to left of 10 and right of 90

P1 ft ft if ogive shape
C1
1 ft
2
Ogive shape
ft if ogive shape
M1 for evidence of reading from $y=20$ and 60 (both 2 and M1 dep on ogive shape)

RECOGNISING ACHIEVEMENT

RECOGNISING ACHIEVEMENT
June 2000
1662/05 Mathematics Syllabus A

| 1 | Line parallel to house wall 2 cm away 'Circular' ends radius 2 cm <br> Circle centre * <br> Radius 2.5 cm <br> Correct shading | $\begin{aligned} & \text { B1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \\ & \text { M1 } \\ & \text { A1 } \\ & \\ & \sqrt{1} \end{aligned}$ | Accuracy $\pm 2 \mathrm{~mm}$, accept dotted lines <br> At least as long as width of house by eye Intention <br> Accurate <br> Intention <br> Accurate, must reach line <br> ft only If M1 gained for circle and there is a line parallel to house <br> Good freehand can score B0,M1,A0,M1,A0,1 $\sqrt{ }$ | 6 |
| :---: | :---: | :---: | :---: | :---: |
| 2 | (a) 24000 <br> (b) 22098.1 <br> (c) 15.5 or $15.4 \dot{9}, 14.5$ | 2 $2 \sqrt{ }$ 2 | M1 for 40 or 30 or 20 SC1 for $43 \times 29 \times 18=22446$ with working shown <br> Ft from figs 24 only, $24 \rightarrow 22.1,240 \rightarrow 221.0$ etc $\mathrm{B} 1 \sqrt{ }(\mathrm{ft}$ from figs 24$)$ for 22098.096 <br> B1 for one correct in correct place or for two correct in wrong places |  |
| 3 | (a) Correct Sample Space with scores or list of ordered pairs <br> 5/36 <br> (b) $30 / 36$ oe or $(\mathrm{n}-6) / \mathrm{n}$ WWW <br> (c) $6 / 36$ oe or $6 / \mathrm{n}$ WWW | M2 <br> A1 <br> $2 \sqrt{ }$ $1 V^{\prime}$ | -1 once for 5 in 36 etc, ISW for cancelling / decimal errors <br> B1 for one or two errors M1 for sample space with points only +A1 for scores of 6 ringed SC2 for 5/36 Without list of outcomes <br> Where $\mathrm{n}=$ number of outcomes in (a) B1 $\sqrt{ }$ for $6 / 36$ or $6 / n$ seen | 12 |
| 4 | (a) $\mathrm{t}^{6}$ <br> (b)(i) $x=3.5$ oe <br> (ii) $x>2.5$ oe $\left(2^{4} / 8\right.$ or better $)$ <br> (c) $(2 x+5)(2 x-5)$ <br> (d)(i) $(x+1)(x+6)$ oe <br> (ii) -1 and -6 | 1 3 2 2 2 | M1 for $3 \mathrm{x}-3=\mathrm{x}+4$ <br> + M1 for $3 \mathrm{x}-\mathrm{x}=4+3$ <br> M1 for $x>20 / 8$ soi <br> SC1 for $(\mathrm{x}=) 2.5, \mathrm{x}<2.5, \mathrm{x} \geq 2.5, \mathrm{x} \leq 2.5$ <br> B1 for $(a x+b)(a x-b)$ seen <br> B1 for factors which would give 2 of the 3 terms <br> Ft from their factors | 11 |


| 5 | (a) (3) $10214973 \quad 9098 \quad 100$ <br> (b) 9 points plotted correctly Curve or straight lines <br> (c) 78 to 82 <br> (d) 1.7 to 2.2 | $\begin{gathered} 1 \\ \sqrt{P 2} \\ \sqrt{G 1} \\ \\ 1 \sqrt{ } \\ 2 \end{gathered}$ | $\pm 1 / 2$ small sq, P1 $\sqrt{ }$ for 7 or 8 correct <br> $\pm 1 / 2$ small sq <br> ft only if no number in table is less than previous one <br> whole number only <br> M1 for attempt to read off both quartiles onto height axis. |  |
| :---: | :---: | :---: | :---: | :---: |
| 6 | Ruled line through $(0,0)$ and $(2,6)$ <br> Ruled line through $(0,6)$ and $(4,0)$ <br> Correct region, including some in -ve x region | 1 <br> 2 <br> $1 \sqrt{ }{ }^{\prime}$ | condone dotted lines <br> $\pm 1$ small square at those points <br> $\pm 1$ small square at those points <br> $\mathbf{S C} 1$ for line through either (not $y=6$ or $x=4$ ) <br> Ft provided first line has positive gradient and second has negative gradient. | 11 |
| 7 | 20 and 16 seen <br> 2 complete correct corresponding ratios / fractions reducing these to comparable forms not same, not similar | $\begin{gathered} \mathbf{B 1} \\ \text { M1 } \\ \text { A1 } \\ \text { A1 } \end{gathered}$ | e.g. 2lengths, 2 widths or length \& width and length \& width <br> dep on M1 only (condone not congruent ) <br> SC2 for complete correct argument using 1 border only <br> Area scale factor + 1.s.f + w.s.f.: M1,A0,A1 <br> Area scale factor +1. .s.f (or w.s.f.) only: $\mathrm{M} 0, \mathrm{~A} 0, \mathrm{~A} 0$ |  |
| 8 | (a) 8 <br> (b) 2 <br> (c) 6 | $\begin{aligned} & 1 \\ & 1 \\ & 1 \\ & \hline \end{aligned}$ |  | 7 |
| 9 | (a) $x>-3$ or $-3<x$ <br> (b)(i) $-1 \frac{1}{2}$ or 1 <br> (ii) U shaped Parabola crossing x axis twice Intersections indicated at their $-1 \frac{1}{2}$ and 1 | 3 <br> 3 <br> M1 <br> A1 $\sqrt{ }$ | M1 for $2 \mathrm{x}-5 \mathrm{x}<12-3$ oe <br> + A1 for $-9<3 x$ or $-3 x<9$ <br> or SC1 for $-3, x=-3, x<-3, x \geq-3, x \leq-3$ <br> M2 for $(2 x+3)(x-1)(=0)$ or $(-1 \pm \sqrt{25}) / 4$ Or $x+1 / 4= \pm \sqrt{ }(25 / 16)$ <br> SC1 for $x=1 \frac{1}{2}$ or -1 or one correct answer <br> SC1 for inverted parabola with intersections at their $-1 \frac{1}{2}$ and 1 . <br> Labelled or good scale |  |


| 10 | (a)(i) $18000 \pi$ <br> (ii) 45 <br> (b) 24 | 2 $2 \sqrt{ }$ $3$ | M1 for ( $4 / 3$ ) $\times \pi \times 30^{3} \div 2$ or better, $\div 2$ can come later. $30^{3}$ can be implied by figs 27 <br> ft is for their 18000 (single number) $\div 400(2 \mathrm{sf})$ M1 for $\pi \times 20^{2} \times h=$ their (a)(i) <br> B1 for 18 seen <br> + M1 for $\sqrt{ }\left(30^{2}\right.$ - their $\left.18^{2}\right)$ or mention of 3,4,5 triangle. | 15 |
| :---: | :---: | :---: | :---: | :---: |
| 11 | (a) $42 / 380$ oe <br> (b) $226 / 380$ oe | 3 4 | -1 once for 5 in 36 etc, ISW for cancelling / decimal errors <br> M2 for $7 / 20 \times 6 / 19$ <br> SC1 for 49/400 <br> M2 for $11 / 20 \times 7 / 19+11 / 20 \times 2 / 19+7 / 20 \times$ <br> $2 / 19$ soi by $113 / 380+$ M1 for $\times 2$ <br> or M3 for complete alternative methods <br> Or B2 for $154 / 380$ seen <br> Or SC1 for 226/400 oe <br> Or if 0 or 1 scored for whole question give M2 for correct tree diagram with probabilities (conditional / unconditional) (NOT + M2) |  |
| 12 | $\begin{aligned} & 35.55 \text { or } 35.549(\mathrm{~m}) \text { or } 3555 \mathrm{~cm} \\ & \text { or } 35 \mathrm{~m} 55(\mathrm{~cm}) \end{aligned}$ | 2 | M1 for $\mathrm{m}-\mathrm{n}$ where $50<\mathrm{m} \leq 50.5$ and $14.5 \leq n<15$ <br> Or SC1 for 15.05 or 14.95 seen |  |
| 13 | (a)(i) $6 \sqrt{ } 2$ <br> (ii) $10 \sqrt{3}$ <br> (iii) $5 \sqrt{3}$ <br> (b) $a=32, b=10$ | 1 <br> 2 <br> 2 <br> 2 | Condone eg $6 \times \sqrt{2}$ <br> B1 for $\sqrt{300}$ or $2 \sqrt{5} \times \sqrt{5} \cdot \sqrt{3}$ or $5 \sqrt{ } 4 \times \sqrt{3}$ seen <br> B1 for any two of $5 \sqrt{2}, 3 \sqrt{3}, 3 \sqrt{2}$ or for $\sqrt{75}$ seen. Condone $5 \sqrt{ } 3 / 1$ <br> B1 for either, $\mathbf{S C 1}$ for $32+10 \sqrt{7}$ seen | 16 |


| 14 | (a) Strata identified <br> Method within strata $10 \%$ clear <br> (b) Ensures all streets, areas etc represented <br> (c) people not on telephone, ex directory, includes businesses etc Or may mean streets / areas etc not represented | M1 <br> A1 <br> A1 <br> 1 <br> 1 | streets, areas etc Must be obtainable without visiting houses accept random or systematic <br> Must refer back to their strata <br> Must refer back to their strata |  |
| :---: | :---: | :---: | :---: | :---: |
| 15 | (a) $\frac{540}{x}+\frac{300}{x+1}=90$ <br> $\div 30$ oe <br> (b) $x=9$ and $-2 / 3$ <br> Final answer 9 | 1 <br> 1 <br> 6 <br> 1 | Dep. Must include some indication of method e.g. intermediate stage with 10 cancelled <br> Accept working in part (a) <br> M2 for $18(x+1)+10 x=3 x(x+1)$ soi or <br> M1 for common denominator $x(x+1)$ <br> + B1 for $28 \mathrm{x}+18$ soi or $3 \mathrm{x}^{2}+3 \mathrm{x}$ seen (indep) <br> + A1 for $3 \mathrm{x}^{2}-25 \mathrm{x}-18(=0)$ or <br> $-3 x^{2}+25 x+18$ <br> $+\mathbf{A 1}$ for $(3 x+2)(x-9)$ oe or subst in formula <br> Answer without working gets final mark only. Independent | 14 |
| 16 | (a) 2 a <br> (b)(i) $\overrightarrow{\mathrm{AB}}=\mathbf{b}-\mathbf{a}$ <br> (ii) $\overrightarrow{\mathrm{CD}}=2 \mathrm{~b}-2 \mathrm{a}$ <br> A further step indicating $C D$ parallel to AB <br> (iii) CD is twice as long as AB $\text { (c) } \begin{aligned} \overrightarrow{\mathrm{AE}} & =\overrightarrow{\mathrm{AC}}+1 / 2 \overrightarrow{\mathrm{CD}} \mathrm{oe} \\ & =\text { b WWW } \end{aligned}$ | 1 1 2 1 1 1 1 M1 A1 | Condone omission of vector marks <br> Condone $\mathbf{a}+\mathbf{a}$ <br> B1 for $\overrightarrow{\mathrm{OD}}=2 \mathrm{~b}$ soi <br> e.g. $\overrightarrow{\mathrm{CD}}=2 \overrightarrow{\mathrm{AB}}, \overrightarrow{\mathrm{CD}}=2(\mathbf{b}-\mathbf{a}), \overrightarrow{\mathrm{CD}}$ is a multiple of $\overrightarrow{A B}$ <br> Indep, Accept $C D=2 A B$ <br> e.g. $\overrightarrow{\mathrm{AE}}=\mathbf{a}+1 / 2(2 \mathbf{b}-2 \mathbf{a}), \overrightarrow{\mathrm{AE}}=\mathbf{a}+\mathbf{b}-\mathbf{a}$ Accept equivalent method finding $\overrightarrow{\mathrm{BE}}=\mathbf{a}$ If $\overrightarrow{A E}$ and $\overrightarrow{B E}$ found both must be correct for $A$ mark | 8 |

RECOGNISING ACHIEVEMENT

Markscheme 1662/6 June 2000

| 1 | (a) Negative <br> (b) Line ruled <br> (c) (i) 9.9 to 10.1 <br> (ii) Time may not continue to decrease with age oe | $\begin{array}{\|l} 1 \\ 1 \\ 1 \\ 1 \\ \hline \end{array}$ | Ignore embellishments <br> Must have at least 3 points on each side and when $x=9,13.5<y<14$ <br> Must indicate why the trend changes or the correlation could change at 18 |
| :---: | :---: | :---: | :---: |
| 2 | (a) (i) $7.6149(0 \ldots)$ <br> (ii) 7.61 <br> (b) Rounds to $\frac{4^{2}(+0.5)}{4 \times 0.5} \text { o.e. or } \frac{4^{2}+0.53}{4 \times 0.5}$ <br> 8 to 8.3 | $\begin{array}{\|l\|} \hline 1 \\ 1 \mathrm{ft} \\ 1 \\ 1 \\ \hline \end{array}$ | Ft from (a)(i) which must be at least $3 \mathrm{~d} . \mathrm{p}$. <br> SC 1 for $\frac{4^{2}+1}{4(\times 1)}$ or $\frac{4^{2}+1}{4 \times 0.5}$ <br> dep. on rounding seen in num and denom |
| 3 | Correct trial for $4 \leqslant x \leqslant 5$ <br> Improved correct trial for $4<x<5$ <br> Trial $4.2<x \leqslant 4.25$ or trials for both 4.2 and 4.3 with a conclusion <br> Answer 4.2 | 1 1 <br> 1 1 | All trials evaluated correctly to the first 2 figs rounded or truncated |
| 4 | (a) 8.9 to 8.94 <br> (b) 7.7 to 7.75 <br> (Answer of 6.67 implies M2 as has used grads) | $3$ $13$ | M2 for $\sqrt{\left(12.4^{2}-8.6^{2}\right)}$  <br> or M1 for $x^{2}+8.6^{2}=12.4^{2}$  <br> M2 for $8.6 \tan (180-138)$ or Or equivalent <br> M1 for $\tan (180-138)=\frac{D C}{8.6}$ oe. trig |
| 5 | (a) (i) 0.72 oe <br> (ii) 0.02 oe <br> (b) (i) 52.25 not $40<t \leqslant 60$ 20.97 to 21 <br> (c) (i) $4,23,53,71,80$ <br> (ii) correct points ft at $20,40,60,80,100$ curve or ruled joins for at least 4 plots <br> (iii) $\frac{13 \pm 1}{80}$ oe or 0.15 to 0.175 | $\begin{array}{\|l\|} \hline 2 \\ 2 \\ 2 \\ 2 \\ 3 \\ 1 \\ 1 \\ \text { Plft } \\ \mathrm{Clft} \\ 2 \mathrm{ft} \\ \hline \end{array}$ | M1 for $0.9 \times 0.8$ <br> B1 for both 0.1 and 0.2 seen <br> M1 for $\Sigma \mathrm{f} x$ midpoints ( $=4180$ ) or 4140 or 4220 (condone 1 error seen) M1 for oe 35195 or $253600 / 80$ <br> And M1 dep for $\div 80$ and root or $-(\bar{x})^{2}$ and $\sqrt{ }$ <br> Ogive shape Ogive shape ignore blocks <br> $1 / 2 \mathrm{sm}$ sq accuracy <br> B1 for $13 \pm 1 \mathrm{ft}$ from ogive |
| 6 | (a) $\mathrm{n}^{2}+1$ seen <br> (b) $4 n^{2}$ or $(2 n)^{2}$ oe unsimplified seen without further error | 2 | B1 for $n^{2}+k$ seen - condone other variable <br> Bl for $k n^{2}$ soi or $2 n$ seen - condone other variable for $k \neq 1$ <br> After $0,0 \mathrm{SCl}$ if quadratic expression seen in (a) or (b). |
| 7 | (a) $83.6^{\circ}$ to $84^{\circ}$ <br> (b) 1.125 cao | 4 | B3 for $41.8^{\circ}$ to $42^{\circ}$ or M3 for $2 \sin ^{-1}\left(\frac{0.8}{1.2}\right)$ implied by $92.9(1 \ldots)$ or M2 for $\sin ^{-1}\left(\frac{0.8}{1.2}\right)$ implied by $46.4(5 \ldots$ or M1 for $\sin x=\frac{0.8}{1.2}$ <br> All M marks available for equivalent trig eg cos rule M1 for $\frac{x}{1.8}=\frac{1}{1.6}$ oe implied by 1.12 or 1.13 |


| 8 | (a) $3 x(2 x-3 y)$ or $-3 x(-2 x+3 y)$ as final answer <br> (b) $0.44(3 \ldots)$ <br> and $-1.69(3 \ldots)$ or -1.7 | 2 | Condone missing final bracket <br> B1 for $x(6 x-9 y)$ or $3\left(2 x^{2}-3 x y\right)$ <br> Or $6 x(x-1.5 y)$ or $3 x(2 x-3 y)$ <br> Or $-3 x(-2 x+3 y)$ seen <br> M1 for $\frac{-5 \pm \sqrt{p}}{8}$ seen and M1 for $\sqrt{73}$ seen - only one correct answer implies M0 M1 |
| :---: | :---: | :---: | :---: |
| 9 | (a) 376 <br> (b) 5 www | 3 | M2 for $\frac{319.6}{0.85}(\times 100)$ soi by figs 376 <br> or M1 for $85 \%=319.6$ <br> or M1 for $k-k \times \frac{15}{100} \approx 319.6$ for $k>368$ <br> M1 for $10 \times 1.15^{n} n>1$ or any one of 13.225 , $15.20875,17.490063,20.113572$ rounded or truncated |
| 10 | (a) multiplication and subtraction or substitution $\begin{aligned} & x=3 \\ & y=-1 / 2 \\ & \hline \end{aligned}$ | M1 <br> A1 <br> A1 | SC2 for both correct but no valid algebraic manipulation |
|  | (b) $y=-6 x+2 \mathrm{www}$ | 4 | Either M1 rise $\div$ run OR <br> A1 $a=-6$ $8=-1 a+b \mathrm{M} 1$  <br> M1 sub coord $-10=2 a+b \mathrm{M} 1$  <br> or attempt at <br> $y$ intercept <br> A1 $b=2$ $a=-6 \mathrm{Al}$  <br>  $b=2 \mathrm{Al}$  |
| 11 | (a) (i) 55 <br> (ii) 35 <br> (iii) 80 <br> (b) (i) $54^{\circ}$ <br> (ii) $22^{\circ}$ | $\begin{array}{\|l\|} \hline 1 \\ 1 \\ 1 \mathrm{ft} \\ 1 \\ 2 \\ \hline \end{array}$ | If ans space blank all marks can be earned for diagram if clear ft for $180-(65+$ their 35 ) <br> B1 for OXT (or OYT) $=90$ seen, can be in diagram |
| 12 | (a) $\frac{4 y-3 x}{4 x}$ oe Accept $\frac{5 y-3 x-y}{4 x}$ <br> (b) $\frac{4 y}{4 a+3}$ oe Accept $\frac{5 y-y}{4 a+3}$ <br> Mark final answers | 3 <br> 3 | M1 for $4 a x=4 y-3 x$ oe and M1 for division by $4 x$ <br> M1 for $4 a x+3 x=4 y$ oe and M1 for $x(4 a+3)=4 y$ oe |
| 13 | (a) $\frac{35}{99}$ o.e. <br> (b) Numbers must be between 1 and 10 eg $\sqrt{2}$ and $\sqrt{8} ; \pi$ and $\frac{6}{\pi}$ | 2 | M1 for complete correct method <br> B1 for any two different irrationals eg $\pi$ and $\frac{3}{\pi}$ |
| 14 | (a) $\frac{3}{10}$ oe www <br> (b) $\frac{1}{20}$ oe www <br> (c) $\frac{1}{10}$ oe www | 2 2 3 | M1 for $\frac{3}{5} \times \frac{2}{4}$ M marks lost if further incorrect method <br> M1 for $\frac{3}{5} \times \frac{2}{4} \times \frac{1}{3} \times \frac{1}{2}$ <br> M2 for $\frac{3}{5} \times \frac{1}{4} \times \frac{2}{3} \times \frac{1}{2}\left(\times \frac{1}{1}\right) \times 2$ or $\frac{2}{5} \times \frac{1}{4}$ <br> Or $\frac{3}{5} \times \frac{2}{4} \times \frac{2}{3} \times \frac{1}{2}\left(\times \frac{1}{1}\right)$ <br> Or MI for $\frac{3}{5} \times \frac{1}{4} \times \frac{2}{3} \times \frac{1}{2}\left(\times \frac{1}{1}\right)$ oe <br> OR M1 for $\frac{1}{5} \times \frac{1}{4}$ or SC1 for KNKNK only selection |


| 15 | $\begin{array}{\|l} \hline 605 \div \text { their } 15 \\ 15.25 \text { or } 15.249 \text { seen } \\ 39 \text { or } 40 \text { www } \\ \hline \end{array}$ | $\begin{aligned} & \text { M1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | If 0 scored SCl for $615 \div 14.75$ or $614.9 \div 14.75$ |
| :---: | :---: | :---: | :---: |
| 16 | $\begin{aligned} & 1 / 2 \times 61 \times 76 \sin A=2300 \\ & \text { or } \sin A=60.526316 \div 61 \\ & A=82.85 \text { to } 83 \\ & 61^{2}+76^{2}-2 \times 76 \times 61 \cos (\text { their } A \text { ) } \\ & \text { for square root but not } \sqrt{k \cos A} \\ & \\ & 91.3 \text { to } 91.5 \\ & 91 \\ & { }^{\text {ccan be earned if } A \text { is not calculated }} \\ & \hline \end{aligned}$ | M1 A1 *M1 *M1 dep A1 B1ft | $\qquad$ Alternative method $\mathrm{AN}=\sqrt{61^{2}-\mathrm{H}^{2}}$ where N is foot of perpendicular from B $\mathrm{AN}=7.5 \text { to } 7.6$ <br> 76 - their AN $\sqrt{(76-\text { their } \mathrm{AN})^{2}+\mathrm{H}^{2}}$ <br> Rounding to nearest whole number or 2 sf |
| 17 | (a) <br> 18.8 to $19.6 \ldots$ <br> (b) <br> 55 to 95 or 0.9 to 1.6 <br> $\mathrm{km} / \mathrm{h}^{2}$ oe or $\mathrm{km} / \mathrm{h} / \mathrm{min}$ oe | M1 <br> M1 <br> M1 <br> A1 <br> M1 <br> M1 <br> dep <br> A1 <br> 1 | For width of 0.25 soi possibly from graph <br> For 5.5 to $6.5,18,18.5,17$ to $17.5,16.5$ to 17 and <br> final $s=0$ to 1.5. Condone one minor error if answer in range. <br> For completely correct method with their heights and $w=0.25$ <br> After 0 scored allow SCl for one correct trapezium <br> For tangent at $t=0.25$ drawn <br> Rise $\div$ run attempted with correct scales <br> Must be consistent with their acceleration. If no acceleration accept $\mathrm{km} / \mathrm{h}^{2}$. |

Markscheme 1662/7 June 2000

MiARKING GUIDE This guide gives examples of the evidence that candidates may produce. MILLENNIUM PARTIES

| MARK FOR EACH STRAND | Strategy | Communication | Reasoning |
| :---: | :---: | :---: | :---: |
| 1 | - Candidates try different approaches and find ways of overcoming difficulties that arise when they are solving problems. They are beginning to organise their work and check results. <br> eg Draws correct arrangement of two square tables to achieve 8 and 6 people. | - Candidates discuss their mathematical work and are beginning to explain their thinking. They use and interpret mathematical symbols and diagrams. <br> Diagrams are clear and convey meaning well [using two tables.] | - Candidates show that they understand a general statement by finding particular examples that match it. <br> eg. Provides more than one answer to the number of people who can sit at a set number of tables. |
| 2 | - Candidates are developing their own strategies for solving problems and are using these strategies both in working within mathematics and applying mathematics to practical contexts. <br> Draws a number of different arrangements of three tables and correctly counts the number of people in most cases. | - Candidates present information and results in a clear way, explaining the reasons for their presentation. <br> Diagrams are clear and convey meaning well [using three tables.] Number of people sitting are recorded. i.e. C1 + Number of people. | - Candidates search for a pattern by trying out ideas of their own. <br> Provides at least three different results for any chosen situation. eg three results for people sitting at three tables. |
| 3 | - In order to carry through tasks and solve mathematical problems, candidates identify and obtain necessary information; they check their results, considering whether these are sensible. <br> eg Draws at least three, correct, different arrangements of tables that will seat 16 people. | - Candidates show understanding of situations by describing them mathematically using symbols, words and diagrams. <br> Tabulates results from diagrams but provides only limited text. i.e. section headings, "I have found...", or "I predict ...." statements. | - Candidates make general statements of their own, based on evidence they have produced, and give an explanation of their reasoning. <br> eg. States that a maximum number of people increases by two or equivalent of $2 n+2$ OR any "correct" generalisation that follows from their results. |
| 4 | - Candidates carry through substantial tasks and solve quite complex problems by breaking them down into smaller, more manageable tasks. <br> eg Gathers adequate correct data by drawing systematic table arrangements and makes any correct general statement to answer the "Maximum number of people" problem. | - Candidates interpret, discuss and synthesise information presented in a variety of mathematical forms. Their writing explains and informs their use of diagrams. <br> Presents a comprehensive record of work involving clear diagrams, tabulated results, and a linking commentary. | - Candidates are beginning to give a mathematical justification for their generalisations; they test them by checking particular cases. <br> eg states $2 n+2$ and tests this on a new case, or the equivalent. [The test must be supported by a new diagram and not have been used to obtain the formula originally.] |


| 5 | - Starting from problems or contexts that have been presented to them, candidates introduce questions of their own, which generate fuller solutions. <br> eg Begins to examine: <br> number of people on arrangements of tables which are not square, OR conditions where numbers of people are minimised etc and generates sufficient data from which a generalisation could be made. | - Candidates examine critically and justify their choice of mathematical presentation, considering alternative approaches and explaining improvements they have made. <br> eg Uses a graphical representation, giving a reason for doing so OR produces C 4 with a formula and evidence of use. <br> This allows a movement into algebra as an improved communication means, with justification implicit, and this secured by showing use. | - Candidates justify their generalisations or solutions, showing some insight into the mathematical structure of the situation being investigated. They appreciate the difference between mathematical explanation and experimental evidence. <br> eg States $2 n+2$ and explains why this applies, with reference to 2 people on either side of teach table and 1 at each end. |
| :---: | :---: | :---: | :---: |
| 6 | - Candidates develop and follow alternative approaches. They reflect on their own lines of enquiry when exploring mathematical tasks; in doing so they introduce and use a range of mathematical techniques. <br> eg applies difference method algebraically [to solve $2 n+2$ ] and must start from $a x+b$. | - Candidates convey mathematical meaning through consistent use of symbols. <br> eg Produces a formula for the maximum number of people which links number of edges of table to number of tables. i.e. $e(n-2)+2$. (oe.) <br> [e = number of edges on a table, $n=$ number of tables.] | - Candidates examine generalisations or solutions reached in an activity, commenting constructively on the reasoning and logic employed, and make further progress in the activity as a result. <br> eg Collates results for tables with different numbers of sides and generates a composite formula, explaining how the multipliers of " n " are related. |
| $7$ | Candidates analyse alternative approaches to problems involving a number of features or variables. They give detailed reasons for following or rejecting particular lines of enquiry. | Candidates use mathematical language and symbols accurately in presenting a convincing reasoned argument. | Candidates' reports include mathematical Justifications, explaining their solutions to problems involving a number of features or variables. |
| 8 | - Candidates consider and evaluate a number of approaches to a substantial task. They explore extensively a context or area of mathematics with which they are unfamiliar. They apply independently a range of appropriate mathematical techniques. | - Candidates use mathematical language and symbols efficiently in presenting a concise reasoned argument. | - Candidates provide a mathematically rigorous Justification or proof of their solution to a complex problem, considering the conditions under which it remains valid. |

GRAZING LAND MARKING GUIDE This guide gives examples of the evidence that candidates may produce.

| MARK FOR EACH STRAND | Strategy | Communication | Reasoning |
| :---: | :---: | :---: | :---: |
| 1 | - Candidates try different approaches and find ways of overcoming difficulties that arise when they are solving problems. They are beginning to organise their work and check results. <br> eg Candidate draws a circle, even freehand, and shows the position of the peg at the centre. | - Candidates discuss their mathematical work and are beginning to explain their thinking. They use and interpret mathematical symbols and diagrams. <br> eg Candidate records work showing at least one circle with the pegs correctly positioned. | - Candidates show that they understand a general statement by finding particular examples that match it. <br> eg Candidate compares their working to the required $100 \mathrm{~m}^{2}$ and answers appropriately. <br> OR states the land grazed will be a circle (, or a semi circle.) |
| 2 | - Candidates are developing their own strategies for solving problems and are using these strategies both in working within mathematics and applying mathematics to practical contexts. <br> eg Candidate draws "circles" with flattened edges as they approach the fence, OR obtains the area of one circle, by any valid method. | - Candidates present information and results in a clear way, explaining the reasons for their presentation. <br> eg Candidate shows clearly how shapes are changed as they approach the boundaries, OR Shows how areas have been obtained, (possibly by using $\Pi r^{2}$ and substitutions for r .) | - Candidates search for a pattern by trying out ideas of their own. <br> Candidate alters the position of the peg or radius to show at least three different positions, <br> OR collects at least three areas of different circles, hopefully stating the intent of finding an area of $100 \mathrm{~m}^{2}$. |
| 3 | - In order to carry through tasks and solve mathematical problems, candidates identify and obtain necessary information; they check their results, considering whether these are sensible. <br> eg Finds more than two areas using any valid method. | - Candidates show understanding of situations by describing them mathematically using symbols, words and diagrams. <br> eg Candidate uses diagrams and calculations with some comments, such as section headings, table headings or " 1 have found ..." statements. | - Candidates make general statements of their own, based on evidence they have produced, and give an explanation of their reasoning. <br> eg Candidate observes that if the rope length is doubled the area is not doubled oe <br> OR describes accurately the shape of the grazed land at limiting conditions eg quarter circles, semicircles. |
| 4 | - Candidates carry through substantial tasks and solve quite complex problems by breaking them down into smaller, more manageable tasks. <br> Candidate produces clear evidence for relevant areas to include non integer lengths to solve circle and/or semicircle case(s). Allows soln to $n r^{2}=1000$ e. $(r>5.64 \mathrm{~m} \quad r>9.77 \mathrm{~m})$ | - Candidates interpret, discuss and synthesise information presented in a variety of mathematical forms. Their writing explains and informs their use of diagrams. <br> Candidate clearly explains, using diagrams and calculations which are linked with a commentary, how they have solved the circle or semicircle | - Candidates are beginning to give a mathematical justification for their generalisations; they test them by checking particular cases. <br> eg Candidate justifies their generalisations by checking with new calculations (Area Just above and just below $r=5.64$ oe) |


| 5 | - Starting from problems or contexts that have been presented to them, candidates introduce questions of their own, which generate fuller solutions. <br> Candidate changes one new variable eg tether point on barn OR length of barn, OR shape of barn etc and generates sufficient evidence that some conclusion could be made. OR moves into 3D, calculating some volumes of spheres towards a stated aim. | - Candidates examine critically and justify their choice of mathematical presentation, considering alternative approaches and explaining improvements they have made. <br> Candidate improves their presentation and justifies the improvement eg colour codes diagrams or produces spreadsheet printout in tables. <br> OR Begins to work using algebra beyond a simple substitution into $A=\Pi r^{2}$ such as $A=\Pi(r-10)^{2}$ or uses a rearrangement of $A=\Pi r 2$. | - Candidates justify their generalisations or solutions, showing some insight into the mathematical structure of the situation being investigated. They appreciate the difference between mathematical explanation and experimental evidence. eg describes loci that result from their set condition(s), OR solves $\Pi r^{2}=100$ oe, with clear explanation of reasoning. |
| :---: | :---: | :---: | :---: |
| 6 | - Candidates develop and follow alternative approaches. They reflect on their own lines of enquiry when exploring mathematical tasks; in doing so they introduce and use a range of mathematical techniques. <br> Candidate allows tether to increase in length and sums series of semi and quarter circles up to but not exceeding the overlap point, OR extends 3D work to include $1 / 4$ and/or $3 / 4$ of spheres towards a stated aim. | - Candidates convey mathematical meaning through consistent use of symbois. <br> Candidate shows competence with algebra and adapts complex formulae involving two variables eg involving the length of the rope ( $r$ ) and the length of the barn (I) into one formula <br> OR spreadsheet formulae are explained showing a clear understanding of how the spreadsheet was constructed. | - Candidates examine generalisations or solutions reached in an activity, commenting constructively on the reasoning and logic employed, and make further progress in the activity as a result. <br> eg Candidate explains why a corner tether will give a larger grazing area for a given rope length than a central tether and supports this with evidence. |
| 7 | - Candidates analyse alternative approaches to problems involving a number of features or variables. They give detailed reasons for following or rejecting particular lines of enquiry. <br> eg Candidate uses, with explanation, a method that gives an (approximate) area of an overlap, (which goes beyond counting squares, such as trigonometry.) <br> OR uses algebra to express a compound area that requires the use of three variables .. rope, barn length and width, OR Begins work on a problem involving a sphere cut by a plane and calculates volumes. | - Candidates use mathematical language and symbols accurately in presenting a convincing reasoned argument. <br> eg Applies trigonometry to the overlap problem and annotates their solution, <br> OR Uses symbols, all correctly defined, to link three variables with a correct argument to support the construction of the formula. | - Candidates' reports include mathematical justifications, explaining their solutions to problems involving a number of features or variables. <br> eg Explains their solution to an overlap case. <br> OR The writing clearly explains how the formula in S 7 has been obtained. in either case this will probably involve the use of clearly annotated diagrams. |


| 8 | - Candidates consider and evaluate a number of approaches to a substantial task. They explore extensively a context or area of mathematics with which they are unfamiliar. They apply independently a range of appropriate mathematical techniques. <br> Candidate attempts a general solution to calculating overlaps which goes beyond S7 <br> OR Uses purely algebraic methods to solve problems in which areas are the same for different shaped regions, <br> OR Makes significant progress on 3D work in S7. | - Candidates use mathematical language and symbols efficiently in presenting a concise reasoned argument. <br> eg Quadratic equations used to solve problems in $\mathrm{S}^{*}$ with elegant method and annotation, <br> OR Constructs formulae for regions other than circles limited by rectangles that require at least three variables .. triangular barns etc | - Candidates provide a mathematically rigorous justification or proof of their solution to a complex problem, considering the conditions under which it remains valid. <br> eg Explains the construction and use of formulae in the case dealt with in S 8 . |
| :---: | :---: | :---: | :---: |

Some Evidence that may be produced in Response to Grazing Land
These calculations may result from the initial problem, in the first case the circle (FII) and in the second, the semi circle $(I / H)$.

| Length <br> of rope | Area | Step | Length <br> of rope | Area | Step | Length <br> of rope | Area | Step |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 3.14 | 1 | 5 | 78.54 | 0.1 | 5.6 | 98.52 | 0.01 |
| 2 | 12.57 |  | 5.1 | 81.71 |  | 5.61 | 98.87 |  |
| 3 | 28.27 |  | 5.2 | 84.95 |  | 5.62 | 99.23 |  |
| 4 | 50.27 |  | 5.3 | 88.25 |  | 5.63 | 99.58 |  |
| 5 | 78.54 |  | 5.4 | 91.61 |  | 5.64 | 99.93 |  |
| 6 | 113.10 |  | 5.5 | 95.03 |  | 5.65 | 100.29 |  |
| 7 | 153.94 |  | 5.6 | 98.52 |  | 5.66 | 100.64 |  |
| 8 | 201.06 |  | 5.7 | 102.07 |  | 5.67 | 101.00 |  |
| 9 | 254.47 |  | 5.8 | 105.68 |  | 5.68 | 101.36 |  |
| 10 | 314.16 |  | 5.9 | 109.36 |  | 5.69 | 101.71 |  |
| 11 | 380.13 |  | 6 | 113.10 |  | 5.7 | 102.07 |  |


| Length <br> of rope | Area | Step | Length <br> of rope | Area | Step | Length <br> of rope | Area | Step |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1.57 | 1 | 9.3 | 135.86 | 0.1 | 9.7 | 147.80 | 0.01 |
| 2 | 6.28 |  | 9.4 | 138.80 |  | 9.71 | 148.10 |  |
| 3 | 14.14 |  | 9.5 | 141.76 |  | 9.72 | 148.41 |  |
| 4 | 25.13 |  | 9.6 | 144.76 |  | 9.73 | 148.71 |  |
| 5 | 39.27 |  | 9.7 | 147.80 |  | 9.74 | 149.02 |  |
| 6 | 56.55 |  | 9.8 | 150.86 |  | 9.75 | 149.32 |  |
| 7 | 76.97 |  | 9.9 | 153.95 |  | 9.76 | 149.63 |  |
| 8 | 100.53 |  | 10 | 157.08 |  | 9.77 | 149.94 |  |
| 9 | 127.23 |  | 10.1 | 160.24 |  | 9.78 | 150.24 |  |
| 10 | 157.08 |  | 10.2 | 163.43 |  | 9.79 | 150.55 |  |
| 11 | 190.07 |  | 10.3 | 166.65 |  | 9.8 | 150.86 |  |

## This evidence may result from extending the length of the rope from the centre

 point of the barn.| Rope Length | Area | Step | Rope Length | Area | Step |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1.57 | 1 | 17 | 530.93 | 1 |
| 2 | 6.28 |  | 18 | 609.47 |  |
| 3 | 14.14 |  | 19 | 694.29 |  |
| 4 | 25.13 |  | 20 | 786.97 |  |
| 5 | 39.27 |  | 21 | 882.79 |  |
| 6 | 56.55 |  | 22 | 986.46 |  |
| 7 | 76.97 |  | 23 | 1096.42 |  |
| 8 | 100.53 |  | 24 | 1212.65 |  |
| 9 | 127.23 |  | 25 | 1335.18 |  |
| 10 | 157.08 |  | 26 | 1463.98 |  |
| 11 | 191.64 |  | 27 | 1599.07 |  |
| 12 | 232.48 |  | 28 | 1740.44 |  |
| 13 | 279.60 |  | 29 | 1888.10 |  |
| 14 | 333.01 |  | 30 | 2042.04 |  |
| 15 | 392.70 |  |  |  |  |
| 16 | 458.67 |  |  |  |  |

This evidence may result from moving the tether to points 2 m apart along the longest side of the barn, up to the point of overlap.
The tables are for $2 \mathrm{~m}, 4 \mathrm{~m}, 6 \mathrm{~m}, 8 \mathrm{~m}$ and the corner of the barn

| Rope <br> Length | Area |
| :--- | :--- |
| 1 | 1.57 |
| 2 | 6.28 |
| 3 | 14.14 |
| 4 | 25.13 |
| 5 | 39.27 |
| 6 | 56.55 |
| 7 | 76.97 |
| 8 | 100.53 |
| 9 | 128.02 |
| 10 | 160.22 |
| 11 | 197.13 |
| 12 | 238.76 |
| 13 | 285.88 |
| 14 | 339.29 |
| 15 | 398.98 |
| 16 | 464.96 |
| 17 | 537.21 |
| 18 | 615.75 |
| 19 | 701.36 |
| 20 | 794.82 |
| 21 | 896.14 |
| 22 | 1005.31 |
| 23 | 1123.12 |
| 24 | 1250.35 |
| 25 | 1387.01 |
| 26 | 1533.10 |
| 27 | 1688.61 |
| 28 | 1853.54 |
| 29 | 2027.90 |
| 30 | 2211.68 |


| Rope <br> Length | Area |
| :--- | :--- |
| 1 | 1.57 |
| 2 | 6.28 |
| 3 | 14.14 |
| 4 | 25.13 |
| 5 | 39.27 |
| 6 | 56.55 |
| 7 | 77.75 |
| 8 | 103.67 |
| 9 | 134.3 |
| 10 | 169.65 |
| 11 | 209.7 |
| 12 | 254.47 |
| 13 | 303.95 |
| 14 | 358.14 |
| 15 | 417.83 |
| 16 | 483.81 |
| 17 | 556.85 |
| 18 | 637.74 |
| 19 | 726.49 |
| 20 | 823.1 |
| 21 | 927.56 |
| 22 | 1039.87 |
| 23 | 1160.03 |
| 24 | 1288.05 |
| 25 | 1424.71 |
| 26 | 1570.8 |
| 27 | 1726.31 |
| 28 | 1891.24 |
| 29 | 2065.6 |
| 30 | 2249.38 |


| Rope <br> Length | Area |
| :--- | :--- |
| 1 | 1.57 |
| 2 | 6.28 |
| 3 | 14.14 |
| 4 | 25.13 |
| 5 | 40.06 |
| 6 | 59.69 |
| 7 | 84.04 |
| 8 | 113.10 |
| 9 | 146.87 |
| 10 | 185.35 |
| 11 | 228.55 |
| 12 | 276.46 |
| 13 | 329.08 |
| 14 | 386.42 |
| 15 | 449.25 |
| 16 | 518.36 |
| 17 | 594.55 |
| 18 | 678.58 |
| 19 | 770.48 |
| 20 | 870.22 |
| 21 | 977.82 |
| 22 | 1093.27 |
| 23 | 1216.58 |
| 24 | 1347.74 |
| 25 | 1486.76 |
| 26 | 1633.63 |
| 27 | 1789.14 |
| 28 | 1954.07 |
| 29 | 2128.43 |
| 30 | 2312.21 |


| Rope <br> Length | Area |
| :--- | :--- |
| 1 | 1.57 |
| 2 | 6.28 |
| 3 | 14.92 |
| 4 | 28.27 |
| 5 | 46.34 |
| 6 | 69.12 |
| 7 | 96.60 |
| 8 | 128.81 |
| 9 | 165.72 |
| 10 | 207.35 |
| 11 | 253.68 |
| 12 | 304.73 |
| 13 | 361.28 |
| 14 | 424.12 |
| 15 | 493.23 |
| 16 | 568.63 |
| 17 | 650.31 |
| 18 | 738.27 |
| 19 | 833.31 |
| 20 | 936.19 |
| 21 | 1046.94 |
| 22 | 1165.53 |
| 23 | 1291.98 |
| 24 | 1426.28 |
| 25 | 1568.44 |
| 26 | 1718.45 |
| 27 | 1876.32 |
| 28 | 2042.04 |
| 29 | 2216.39 |
| 30 | 2400.18 |


| Rope <br> Length | Area |
| :--- | :--- |
| 1 | 2.36 |
| 2 | 9.42 |
| 3 | 21.21 |
| 4 | 37.70 |
| 5 | 58.90 |
| 6 | 84.82 |
| 7 | 115.45 |
| 8 | 150.80 |
| 9 | 190.85 |
| 10 | 235.62 |
| 11 | 285.88 |
| 12 | 342.43 |
| 13 | 405.27 |
| 14 | 474.38 |
| 15 | 549.78 |
| 16 | 631.46 |
| 17 | 719.42 |
| 18 | 813.67 |
| 19 | 914.20 |
| 20 | 1021.02 |
| 21 | 1134.90 |
| 22 | 1256.64 |
| 23 | 1386.23 |
| 24 | 1523.67 |
| 25 | 1668.97 |
| 26 | 1822.12 |
| 27 | 1983.13 |
| 28 | 2151.99 |
| 29 | 2328.71 |
| 30 | 2513.27 |
|  |  |

Formulas that might result from an algebraic analysis of the problem.
From the centre of the barn
$A=\frac{\Pi r^{2}}{2} \quad r \leq 10$
$A=\frac{\Pi(r-10)^{2}}{2} \quad 10 \leq r \leq 20$
$A=\frac{\square(r-20)^{2}}{2} \quad 20 \leq r \leq 30$
From the centre of any barn, length L, width W
$A=\frac{\Pi(r-L / 2)^{2}}{2}$
$A=\frac{\Pi(r-L / 2-W)^{2}}{2}$
Further formulae may well result from the proportional division of L (and W) as the tether point is moved.

These are the areas of the overlap created when the rope extends from 30 m to 40 m , and the tether is in the middle of the barn. (Areas in $\mathrm{m}^{2}$ )

| Rope <br> Length | Area of Overlap <br> (using an <br> approximation to a <br> triangle) | Area of Overlap <br> (Calculated using a <br> sector of a circle) |
| :---: | :---: | :---: |
| 31 | 4.58 | 6.17 |
| 32 | 13.27 | 18.01 |
| 33 | 24.92 | 34.08 |
| 34 | 39.19 | 53.96 |
| 35 | 55.90 | 77.44 |
| 36 | 74.94 | 104.39 |
| 37 | 96.23 | 134.74 |
| 38 | 119.73 | 168.43 |
| 39 | 145.40 | 205.41 |
| 40 | 173.21 | 245.67 |

## Formulae developed from researching the overlap might be:

$A=\frac{\sqrt{ }\left((r-20)^{2}\right.}{} \frac{-100] \times(r-30)}{2}$
Given that $30 \leq \mathrm{r} \leq 40$
$A=\frac{\sqrt{ }\left((r-L / 2-W)^{2}-100\right] \times(r-(L+W))}{2}$
Given that $L / 2+W \leq r \leq \frac{3 L}{2}+W$
$\theta=\cos -1(10 /(r-20))$
$\left.A=2\left[\Pi(r-20)^{2} \theta\right) / 360-5(r-20) \sin \theta\right]$
$\theta=\cos -1(10 /(r-L / 2-W))$
$\left.A=2\left[\Pi(r-L / 2-W)^{2} \theta\right) / 360-5(r-L / 2-W) \sin \theta\right]$
BAKER'S DOZEN - MARKING GUIDE This guide gives examples of the evidence that candidates may produce.

| MARK FOR EACH STRAND | Strategy | Communication | Reasoning |
| :---: | :---: | :---: | :---: |
| 1 | - Candidates try different approaches and find ways of overcoming difficulties that arise when they are solving problems. They are beginning to organise their work and check results. <br> Attempts to solve the initial problem. | - Candidates discuss their mathematical work and are beginning to explain their thinking. They use and interpret mathematical symbols and diagrams. <br> Shows some record of work done. | - Candidates show that they understand a general statement by finding particular examples that match it. <br> Shows another swap or draws, correctly, an initial arrangement of buns not shown in the task. |
| 2 | - Candidates are developing their own strategies for solving problems and are using these strategies both in working within mathematics and applying mathematics to practical contexts. <br> Correctly solves the first problem, i.e. rearranges the array to give an answer of 3 moves. | - Candidates present information and results in a clear way, explaining the reasons for their presentation. <br> eg Shows an organised record of swaps needed to solve the first problem | - Candidates search for a pattern by trying out ideas of their own. <br> eg Tries at least three sequences of moves to solve an arrangement, or lists at least three moves to look for a pattern. |
| 3 | - In order to carry through tasks and solve mathematical problems, candidates identify and obtain necessary information; they check their results, considering whether these are sensible. <br> Correctly applies swapping method to another case. | - Candidates show understanding of situations by describing them mathematically using symbols, words and diagrams. <br> eg From diagrams [or moves with counters] produces a table of numbers of moves for different numbers of buns and provides some text. <br> i.e. Section headings, "I have found ..." or "I predict ...." statements. | - Candidates make general statements of their own, based on evidence they have produced, and give an explanation of their reasoning. <br> eg States that the number of moves increases by one extra each time OR states Trianguiar Numbers OR shows difference pattern OR $\frac{n(n-1)}{2}$ or $\frac{n(n+1)}{2}$ |
| 4 | - Candidates carry through substantial tasks and solve quite complex problems by breaking them down into smaller, more manageable tasks. <br> Obtains sufficient correct results to soive the initial problem and makes a general statement. eg $3,6,10,15, \ldots . .$. hence, "Goes up by 1 more each time " or "Triangular Numbers are generated" [oe] | - Candidates interpret, discuss and synthesise information presented in a variety of mathematical forms. Their writing explains and informs their use of diagrams. <br> Commentary explains how buns move and how the diagrams are tables of results are related. <br> i.e. C3 with linking commentary. | - Candidates are beginning to give a mathematical justification for their generalisations; they test them by checking particular cases. <br> States that the number of moves is the pattern of Triangular Numbers, or equivalent formula, and tests this on a new number of buns. This test must be supported by result obtained through arranging. |


| 5 | - Starting from problems or contexts that have been presented to them, candidates introduce questions of their own, which generate fuller solutions. <br> States conditions for a personal line of research and obtains sufficient correct results from which a further generalisation could be made. <br> eg Works with three types of bun or moves buns to the "other end" or changes the arrangement AABB. | - Candidates examine critically and justify their choice of mathematical presentation, considering alternative approaches and explaining improvements they have made. <br> Produces evidence for C 4 and states an algebraic formula $n(n-1) / 2$ with evidence of use. (The meaning of $n$ can be implicit from the usage.) | - Candidates justify their generalisations or solutions, showing some insight into the mathematical structure of the situation being investigated. They appreciate the difference between mathematical explanation and experimental evidence. <br> Explains WHY the number of swaps is a Triangular Number showing that buns move $1,2,3, \ldots$ swaps, hence $1+2+3+\ldots=$ Triangular Numbers. |
| :---: | :---: | :---: | :---: |
| 6 | Candidates develop and follow alternative approaches. They reflect on their own lines of enquiry when exploring mathematical tasks; in doing so they introduce and use a range of mathematical techniques. <br> Begins to apply the "Difference Method" algebraically i.e. uses differences to determine a coefficient in $\mathrm{an}^{2}+$ bn + c (must be stated)for their new development. <br> OR Tabulates together previous results with new ones and seeks linkages i.e. Common Factors | - Candidates convey mathematical meaning through consistent use of symbols. <br> eg produces a variant of $n(n-1) / 2$ to satisfy their chosen development. (The meaning of $n$ can be implicit from the usage.) | - Candidates examine generalisations or solutions reached in an activity, commenting constructively on the reasoning and logic employed, and make further progress in the activity as a result. <br> Derives a new formula i.e. $3 n(n-1) / 2$ by examining new and old results and deducing a common multiple. |
| 7 | - Candidates analyse alternative approaches to problems involving a number of features or variables. They give detailed reasons for following or rejecting particular lines of enquiry. <br> Correctly completes Difference Method (fromS6) The resulting formula is evidence for R6. OR Continues to link old and new results, spots linkages and generates further formulae. | - Candidates use mathematical language and symbols accurately in presenting a convincing reasoned argument. <br> eg Correctly annotates Difference Method which must begin $a n^{2}+b n+c$. <br> OR Examines a sequence of formulae for different sets of numbers and argues for the R7 case. | - Candidates' reports include mathematical justifications, explaining their solutions to problems involving a number of features or variables. <br> Derives formula involving three variables eg $\frac{\mathrm{t}(\mathrm{t}-1)}{2} \frac{\mathrm{n}(\mathrm{n}-1)}{2}$ oe. |


| 8 | - Candidates consider and evaluate a number of approaches to a substantial task. They explore extensively a context or area of mathematics with which they are unfamiliar. They apply independently a range of appropriate mathematical techniques. <br> Attempts, with some success, a proof for their chosen development. | - Candidates use mathematical language and symbols efficiently in presenting a concise reasoned argument. <br> Uses efficient language and symbols linked to S8 and to facilitate R8. | - Candidates provide a mathematically rigorous justification or proof of their solution to a complex problem, considering the conditions under which it remains valid. <br> eg Proof of formula being the product of two triangular numbers, oe depending on the development chosen. <br> eg Proof by Induction. |
| :---: | :---: | :---: | :---: |

